

***Cognitively Guided Instruction:
A Selection of Publications
November 2010
Compiled by Linda Levi, Teachers Development Group***

This is a selection of published work related to Cognitively Guided Instruction. Other sources can be found by looking for other work by these authors and in the reference list of these publications.

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Blogs run by members of the CGI team:

Empson, Susan B. *Learning Math, Teaching Math* by at <http://www.edb.utexas.edu/empson/>

Levi, Linda L. *Understanding Children's Mathematic* at <http://www.lindalevi@blogspot.com>

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